Great Expectations: The Pygmalion Effect

Sambit Panda

A Real World View of Applied Math and Statistics

Dr. John Taylor and Mrs. Desiré

Summer Ventures in Science and Mathematics

University of North Carolina Charlotte
Abstract

In the distant past to the present, teachers have always been providing positive reinforcement to their students. However, do these effects actually work? How effectively does positive reinforcement actually affect student’s performance on a test?

These questions are answered by the Pygmalion effect, a social theory that hypothesizes that if positive reinforcement is given to someone, they will most likely perform better on tests or other assignments. This study takes a sample size of 50 students and creates a social experiment where the students are given two tests. After the first test, half of the students are chosen randomly to be in the “top 25” while the other half was not told anything. All the students were given another test again and the results were compiled to assess improvement. Those who were “top 25” performed better on the test then those who didn’t by a very wide margin. This supports the idea behind the Pygmalion effect and has wide educational and social applications.
Background & Research Question

For much of human history, the concept of furthering education has been a centerpiece of civilization. To raise students understanding of topics, teachers have utilized a fairly new phenomenon known as the Pygmalion Effect.

The Pygmalion Effect in short is the idea that if someone is told that they can do better, they will. Consider, for example, a common classroom in which intellectually bright students as well as those not as bright study together. The teacher, seeing greater potential in the students who perform higher, give those students more challenging problems, work with them closer, and give them more positive feedback. Meanwhile, those students who are not “brilliant” are subjected to less scrutiny and are not given as much feedback by the teacher.

Research into this idea was brought into mainstream scientific literature by Robert Rosenthal, a professor at Harvard University. In 1963, he published a paper in the *American Scientist*, summarizing his results. Since then, nearly 345 studies have been conducted to support his hypothesis (Rosenthal & Jacobson, 1980). In his project, Rosenthal, with the aid of social scientist Lenore Jacobson, decided to investigate his theory in a public elementary that was given the pseudonym Oak School. The school was divided into three classes for grades one through six: fast, medium, and slow. A sample size of 370 students was taken from the school and given IQ tests. The teachers were given a list of the top scoring students. When the test was given again at the end of the year, the students who were deemed top scoring showed significant improvement in scores.

However, the “top scoring students” were actually chosen at random. So, the fact that they did better is significant to note. Rosenthal and Jacobson took the study further to not only analyze the students, but the teachers as well. They noticed that the teachers taught the “top”
students differently, giving them more challenging problems, more thorough feedback, and more scrutiny if they were unsure about something. This caused those students to perform significantly higher than the other students and boosted their own overall confidence.

This study supports the bigger idea that people do what they are expected to do, a self-fulfilling prophecy. So, the “top” students were expected to do better and therefore performed better. It is “how one person’s expectation for another person’s behavior can quite unwittingly become a more accurate prediction simply for its having been made” (Rosenthal & Jacobson, p. vii, 1968).

Since 1968, numerous studies have tried to support the same conclusion. Quite recently (2010), Kimberly K. Buryanek completed a dissertation in Iowa State University for her doctorate in philosophy. She performed her experiment in New Horizons High School after they decided to make a commitment to work on reform initiatives. Prior to the reform initiatives, nearly “253 D’s and F’s were earned by high school students during the first semester and 122 D’s and F’s were earned by middle-school students during the same period” (Buryanek, p. 2, 2010). After applying the Pygmalion effect, there was a 89% decrease in grades below a C- during the first semester.

Further studies have been done outside the country. In the Beijing Institute of Petrochemical Technology, Jie Chang did a study on teacher expectations and student achievement. She performed a survey mid-semester to find if students who were held in better regard in English, which is considered a foreign language in China. She found that “teacher motivation and teacher enthusiasm influences student motivation and student performance” (Chang, p. 3, 2011).
From 1968 to the present, studies have been conducted, most supporting, but some unable to find complete evidence of the effect. The effect is in wide use and used by teachers inadvertently to teach children. TIME Magazine recently released an article that identified that there were four specific ways teachers treated those students they had higher expectations of:

1. “They create a warmer ‘socioemotional climate’ for their learners they regard as high potential, often conveying this warmth through non-verbal signals: a nod, an encouraging smile, a touch on the shoulder
2. They teach more material, and more difficult material, to the learners they see as especially promising.
3. They give up-and-coming learners more opportunities to contribute, including additional time to respond to questions
4. They offer their ‘special’ learners feedback on performance that is more detailed and more personalized and no just a generic ‘Good job’” (Paul, 2013)

Finally, the Pygmalion Effect is can also be extended beyond the classroom, as recent research suggests. It has been shown that juries are more likely to say a defendant is guilty if the judge themselves think they are guilty. Similarly, organization effectives can be increased by raising leaders’ expectations. Therefore, this psychological phenomenon can transform not only education, but nearly all walks of life and all professions.

This study intends to provide yet another replicate of Rosenthal’s 1968 experiment. It will utilize Summer Ventures’ students to take an aptitude test and see if encouragement will lead to more improvement in test scores. It will then evaluate those test scores and assess by a hypothesis test whether encouragement in fact leads to better test scores.
Method / Results

To begin collecting data, it was necessary to choose a sample size. Due to time restraints, while maintain a good size, a sample size of 50 was chosen. The test was 10 questions long and had the following proportion of questions:

1. 2 Mathematics Questions (algebra, geometry, general addition and subtraction; AMC Questions)
2. 2 English Questions (SAT sentence completion)
3. 3 Science Questions (1 from physics, chemistry, and biology; SAT subject multiple choice)
4. 2 Social Science Questions (1 from us history and world history; SAT subject multiple choice)
5. 1 Art Question (1 from AP Art History Exam)

Knowing that many of the students who were in different counties had a disproportionate amount of education, it was expected to no one was to get all of the questions right. Such a wide range of topics made it easier to separate out the truly intelligent. A time limit was also added on the test to not only intentionally coerce students to stick with their first answer, but also to rank students from best to worst as they performed on the test.

During the first test, attached in the appendix, the students were given no encouragement. This test was intended to make the students think that the “top 25” among them was going to be chosen and were to perform something special.

Students were chosen actually ordered from top rank to bottom rank in a spreadsheet. Every other score was chosen—most of the time—leading to a higher randomized set of students. Students who were made to think they were top 25 spread the word, bragging that they were at
the top. The “top 25” also received a review session in which the answers to the previous test were given as well as prepping for the upcoming test. This set of students was also given positive encouragement to do better on the next test. Meanwhile, the other set was neither prepped nor encouraged.

After about a day of prepping, the new test was given to see if the students would improve. The same style of test was given, with the same proportions of questions Appendix 3 shows the results of the experiment, by calculating improvement as the first score subtracted from the second score. The first two appendices give the tests and the answers. A summary of the results are shown below:

From the histogram, it is obvious that the majority of the scores (nearly 62%) of the scores lie between 3 and 5 out of 10. Therefore, the distribution for the first test can be assumed to be skew right. To calculate the mean of this sample distribution, the formula is
\[ \bar{x} = \frac{\sum xf}{\sum f} \]

where \( x \) is the sample and \( f \) is the frequency of each. Performing the calculations,

\[ \bar{x} = \frac{4 \times 1 + 3 \times 2 + 11 \times 3 + 9 \times 4 + 11 \times 5 + 6 \times 6 + 5 \times 7 + 1 \times 8 + 0 \times 9 + 0 \times 10}{4 + 3 + 11 + 9 + 11 + 6 + 5 + 1 + 0 + 0} = 4.26 \]

The standard deviation of the set can be found by using the formula

\[ s = \sqrt{\frac{\sum x^2 - (\sum x)^2}{n - 1}} \]

where \( s \) is the standard deviation and \( n \) is the number in the sample. Again performing the calculations,

\[ s = \sqrt{\frac{1059 - 213^2}{10 - 1}} = \sqrt{\frac{1059 - \frac{213^2}{10}}{9}} = 1.75905819 \]

Using these two pieces of data, it is possible to create a normal distribution curve for this data, as shown below.
The results of Test 2 are in the histogram below.

![Scores for Test 2](image)

Calculations can be done similarly above. So,

$$\bar{x} = 4.56 \quad s = 1.864381497$$

Similar to above, a normal distribution graph can be made again.
The hypothesis to test is whether those chosen for the “top 25” do in fact earn higher scores than those who are not. That is,

\[ H_0: \mu_1 \leq \mu_2 \]
\[ H_a: \mu_1 > \mu_2 \]

where \( H_0 \) is the hypothesis, \( H_a \) is the alternative hypothesis, \( \mu_1 \) is the “top 25” mean, and \( \mu_2 \) is the other half’s mean.

For this study, the t standardized statistic must be calculated next for the improvement. This is because the population size is under 30 for each population. The statistic is calculated using the formula:

\[
t^* = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}} \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}
\]

by rearranging the formula for the hypothesis, \( \mu_1 - \mu_2 = 0 \). Also,

\[
\bar{x}_1 = 1.32, \quad \bar{x}_2 = -0.88 \\
n_1 = 25, \quad n_2 = 25 \\
s_1 = 2.055885859, \quad s_2 = 1.763519209
\]

\textit{degree of freedom (d.f.)} = \( n_1 + n_2 - 2 = 25 + 25 - 2 = 48 \)

substituting the values into formula,

\[
t^* = \frac{1.32 - (-0.88)}{\sqrt{\frac{(25 - 1)2.055885859^2 + (25 - 1)1.763519209^2}{25 + 25 - 2}} \sqrt{\frac{1}{25} + \frac{1}{25}}} = 4.061
\]

Utilizing the classical approach, the rejection region lies:
At the $\alpha$-level of .005, it is obvious from this graph that the $t^*$ value is well into the rejection region. Because $t^*$ nearly doubles the actual $t$-table value, it is possible to modify the equation to

$$t^* = \sqrt{\frac{1.32 - (-.88) - .80}{(25 - 1)2.055885859^2 + (25 - 1)1.763519209^2}} \frac{1}{25 + 25 - 2} \frac{1}{\sqrt{\frac{1}{25} + \frac{1}{25}}} = 2.58434029$$

where the modified hypotheses are

$$H_0: \mu_1 - \mu_2 \leq .80$$

$$H_a: \mu_1 - \mu_2 > .80$$

The value falls in the rejection region, and so the hypothesis is rejected. Therefore, at the $\alpha$-level of .005, it is possible to conclude that the “top 25” students show greater improvement because of positive reinforcement in their scores than the other half of the students by nearly 80%. This is monumental, demonstrating that there is more than sufficient evidence to support encouragement helps test taking.
Discussion

As discussed in moderate detail in the previous section, an 80% greater improvement for those who are “top 25” than those who are not is significant. It lends to validation of the Pygmalion Effect and builds upon the results from 1968. It also supports the continuing teaching of teachers to always build positively upon students. Some solutions to the problem is dramatically smaller class sizes and more interactive student involvement. Teachers can also give scores to students individually instead of a ranking of each student’s scores. This can cause less negative reinforcement in the classroom.

There are not only educational applications to this study, but social ones as well. The Pygmalion effect can be extended to the workspace and other institutions as well. For example, offices can utilize the Pygmalion Effect to further worker productivity. Judges should be taught to not determine a defendant’s guilt prior to a trial. Surgeons could use this to even raise nurse productivity in the emergency room. Further studies in this field could revolutionize all walks of life.

Of course, the study had some flaws. It tried to recreate similar testing conditions for each student, but some complained that certain places were louder. It was necessary to have each student to do the test separately to limit cheating, but, because it was not practical to force students to isolate themselves, it was limited as much as possible. Also, some students were rushed because certain events were occurring, so there might have been some guessing. Not knowing the material was limited by providing a complete set of subjects. This is further supported by an almost normal distribution of the data.
References


Appendix 1: Aptitude Test 1 and Answers

1. Let $X$ and $Y$ be the following sums of the arithmetic sequences:

   \[ X = 10 + 12 + 14 + \cdots + 100 \]
   \[ Y = 12 + 14 + 16 + \cdots + 102 \]

   What is the value of $Y - X$?
   
   a. 92  
   b. 98  
   c. 100  
   d. 102  
   e. 112

2. Apparently the groom was very nervous: one moment he would be ____, rambling on to his best man about silly, meaningless things, and then abruptly he would turn ____ and could not be prompted to say anything

   a. garrulous … reticent  
   b. grandiose … taciturn  
   c. vociferous … effusive  
   d. melodious … timorous  
   e. munificent … utilitarian

3. Which of the following statements best represents a nativist attitude toward the influx of immigrants around 1900?

   a. Slavs and Italians will be assimilated as easily into the American way of life as were earlier immigrant groups.
   b. Ellis Island should be enlarged to accommodate the huge influx of immigrants.
   c. Immigrants will work for low wages and break strikes, thereby hurting all American workers.
   d. Native-born Americans should organize to help find jobs and homes for new immigrants so that they can become citizens as quickly as possible.
   e. Political machines in the large cities should be responsible for providing immigrants with food, shelter, and jobs in return for their votes.

4. Cosmologist Martin Rees has cautioned that our present satisfaction with the big bang explanation for the creation of the universe may reflect the ____ of the data rather than the ____ of the theory.

   a. paucity … validity  
   b. genius … accuracy  
   c. relevance … scope
5. The 1907 painting by Picasso shown here reveals the influence of which of the following?

   a. Chinese Art
   b. African Art
   c. Indian Art
   d. Medieval Art
   e. Romantic Art

6. Which of the following is true of the magnetic field produced by a current in a long, straight wire?
   a. The field is uniform
   b. The field increases in strength as the distance from the wire increases
   c. The field lines are directed parallel to the wire, but opposite to the direction of the current
   d. The field lines are directed radially outward from the wire
   e. The field lines form circles about the wire

7. Which of the following was characteristic of the physical environments of early river-valley civilizations in the Near East?
   a. Cool summer temperatures encouraged the production of grain crops
   b. Tropical forests along the riverbanks provided the population with most of its food
   c. The rivers maintained a steady flow year-round, fed by melting mountain glaciers
   d. The rivers flowed through deep mountain valleys, which sheltered early civilizations
   e. Rainfall was low, requiring irrigation of crops with river water

8. Which of the following most accurately reveals common ancestry among many different species of organisms?
   a. The amino acid sequence of their cytochrome C
   b. Their ability to synthesize hemoglobin
   c. The percentage of their body weight that is fat
d. The percentage of their body surface that is used in gas exchange

e. The mechanism of their mode of locomotion

9. Square $ABCD$ has side length 10. Point $E$ is on $\overline{BC}$, and the area of $\triangle ABE$ is 40. What is $BE$?

10. Reaction of silver ion with chloride ion in water solution


Answers

1. a
2. a
3. c
4. a
5. b
6. e
7. e
8. b
9. e
10. a
Appendix 2: Aptitude Test 2 and Answers

1. What is the value of

\[
\frac{2^{2014} + 2^{2012}}{2^{2014} - 2^{2012}}
\]

a. −1   b. 1   c. \(\frac{5}{3}\)   d. 2013   e. 2^{4024}

2. She found that fame was both ________ and ________; not only was it difficult to get her book published, but when she did, members of the media quickly lost interest in it.
   a. destructive...counterproductive
   b. evanescent...gratifying
   c. tedious...deleterious
   d. elusive...ephemeral
   e. fulfilling...subtle

3. Which of the following was true of Black soldiers in the United States Army during the First World War?
   a. Black soldiers and White soldiers served in fully integrated units
   b. Black soldiers served in segregated units often commanded by White officers
   c. Black Americans were drafted into the armed forces but were not allowed to enlist
   d. Black Americans were not allowed in the armed forces, but were encouraged to take factory jobs in war industries
   e. Because some Black leaders opposed the war, the government placed Black soldiers only in noncombat positions

4. The ______ espionage plot was so sophisticated it was impossible to believe it was the work of teenage computer hackers.
   a. simple
   b. vaporized
   c. byzantine
   d. mystical
   e. fusty

5. The structure shown to the left is
   a. A European House
   b. A Japanese House
   c. A European Factory
   d. An American Art Museum
   e. An Indian House
6. An object with mass $m$ and speed $v_0$ directed to the right strikes a wall and rebounds with speed $v_0$ directed to the left. The change in the object's momentum is
   a. $2mv_0$ directed to the left
   b. $mv_0$ directed to the left
   c. 0
   d. $mv_0$ directed to the right
   e. $2mv_0$ directed to the right

7. The Silk Routes were important in ancient times because they
   a. Facilitated the exchange of goods and ideas between China and the Roman Empire
   b. Allowed gold and silver mined in China to be traded for European furs and wool cloth
   c. Provided trade links between the people of Siberia and the people living on islands in the Bering Sea
   d. Provided a conduit for trade in silk, porcelain, and costly gems between China and Japan
   e. Allowed carts and carriages to travel on paved roads across northern Asia as far west as the Caspian Sea

8. Nitrogenous base that occurs in RNA but not in DNA
   a. Deoxyribose
   b. Ribose
   c. Uracil
   d. Cytosine
   e. Thymine

9. Define $x\#y$ to be $|x - y|$ for all real numbers $x$ and $y$. Which of the following statements is not true?
   a. $x\#y = y\#x$ for all $x$ and $y$
   b. $2(x\#y) = (2x)\#(2y)$ for all $x$ and $y$
   c. $x\#0 = x$ for all $x$
   d. $x\#x = 0$ for all $x$
   e. $x\#y > 0$ if $x \neq y$

10. From their electron configurations, one can predict that the geometric configuration for which of the following molecules is NOT correct?
    a. PF$_3$, trigonal planar
    b. CF$_4$, tetrahedral
    c. CHCl$_3$, irregular tetrahedron
    d. OF$_2$, bent (v-shaped)
    e. HF, linear

Answers
1. c
2. d
3. b
4. c
5. a
6. a
7. a
8. c
9. c
10. a
### Appendix 3: Chart of Student Results

<table>
<thead>
<tr>
<th>Student #</th>
<th>Score Test 1</th>
<th>Score Test 2</th>
<th>Improvement</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>8</td>
<td>6</td>
<td>-2</td>
</tr>
<tr>
<td>2</td>
<td>7</td>
<td>4</td>
<td>-3</td>
</tr>
<tr>
<td>3</td>
<td>7</td>
<td>6</td>
<td>-1</td>
</tr>
<tr>
<td>4</td>
<td>7</td>
<td>6</td>
<td>-1</td>
</tr>
<tr>
<td>5</td>
<td>7</td>
<td>4</td>
<td>-3</td>
</tr>
<tr>
<td>6</td>
<td>7</td>
<td>7</td>
<td>0</td>
</tr>
<tr>
<td>7</td>
<td>6</td>
<td>4</td>
<td>-2</td>
</tr>
<tr>
<td>8</td>
<td>6</td>
<td>2</td>
<td>-4</td>
</tr>
<tr>
<td>9</td>
<td>6</td>
<td>6</td>
<td>0</td>
</tr>
<tr>
<td>10</td>
<td>6</td>
<td>3</td>
<td>-3</td>
</tr>
<tr>
<td>11</td>
<td>6</td>
<td>8</td>
<td>1</td>
</tr>
<tr>
<td>12</td>
<td>6</td>
<td>4</td>
<td>-2</td>
</tr>
<tr>
<td>13</td>
<td>5</td>
<td>8</td>
<td>3</td>
</tr>
<tr>
<td>14</td>
<td>5</td>
<td>5</td>
<td>0</td>
</tr>
<tr>
<td>15</td>
<td>5</td>
<td>5</td>
<td>0</td>
</tr>
<tr>
<td>16</td>
<td>5</td>
<td>2</td>
<td>-3</td>
</tr>
<tr>
<td>17</td>
<td>5</td>
<td>5</td>
<td>0</td>
</tr>
<tr>
<td>18</td>
<td>5</td>
<td>4</td>
<td>-1</td>
</tr>
<tr>
<td>19</td>
<td>5</td>
<td>5</td>
<td>0</td>
</tr>
<tr>
<td>20</td>
<td>5</td>
<td>4</td>
<td>-1</td>
</tr>
<tr>
<td>21</td>
<td>5</td>
<td>5</td>
<td>0</td>
</tr>
<tr>
<td>22</td>
<td>5</td>
<td>4</td>
<td>-1</td>
</tr>
<tr>
<td>23</td>
<td>5</td>
<td>8</td>
<td>3</td>
</tr>
<tr>
<td>24</td>
<td>4</td>
<td>2</td>
<td>-2</td>
</tr>
<tr>
<td>25</td>
<td>4</td>
<td>2</td>
<td>-2</td>
</tr>
<tr>
<td>26</td>
<td>4</td>
<td>5</td>
<td>1</td>
</tr>
<tr>
<td>27</td>
<td>4</td>
<td>4</td>
<td>0</td>
</tr>
<tr>
<td>28</td>
<td>4</td>
<td>3</td>
<td>-1</td>
</tr>
<tr>
<td>29</td>
<td>4</td>
<td>4</td>
<td>0</td>
</tr>
<tr>
<td>30</td>
<td>4</td>
<td>3</td>
<td>-1</td>
</tr>
<tr>
<td>31</td>
<td>4</td>
<td>8</td>
<td>4</td>
</tr>
<tr>
<td>32</td>
<td>4</td>
<td>5</td>
<td>1</td>
</tr>
<tr>
<td>33</td>
<td>3</td>
<td>7</td>
<td>4</td>
</tr>
<tr>
<td>34</td>
<td>3</td>
<td>5</td>
<td>2</td>
</tr>
<tr>
<td>35</td>
<td>3</td>
<td>6</td>
<td>3</td>
</tr>
<tr>
<td>36</td>
<td>3</td>
<td>4</td>
<td>1</td>
</tr>
<tr>
<td>37</td>
<td>3</td>
<td>4</td>
<td>1</td>
</tr>
<tr>
<td>38</td>
<td>3</td>
<td>2</td>
<td>-1</td>
</tr>
<tr>
<td>39</td>
<td>3</td>
<td>5</td>
<td>2</td>
</tr>
<tr>
<td>40</td>
<td>3</td>
<td>7</td>
<td>4</td>
</tr>
<tr>
<td>41</td>
<td>3</td>
<td>1</td>
<td>-2</td>
</tr>
<tr>
<td>42</td>
<td>3</td>
<td>1</td>
<td>-2</td>
</tr>
</tbody>
</table>
(Note: Tests were given anonymously many students did not want their results to be displayed. Thus, each student is given a number to represent their name. Also, students in yellow are “top 25” and were encouraged)